

# A COMBINED EXPERIMENTAL AND THEORETICAL CHARACTERISATION OF DISCONTINUITIES IN UNILATERAL FINLINES

Adalbert Beyer, Dietmar Köther and Ingo Wolff

Department of Electrical Engineering, Duisburg University,  
Bismarckstraße 81, D-4100 Duisburg 1, FRG

## Abstract

An optimization procedure for characterizing finline discontinuities has been developed using the generalized scattering matrix formulation for steps in finline technique. The general waveguide representation of a two-taper finline section with a step is investigated first. The scattering matrix representation of the step is deduced from a combined measurement-numerical optimization procedure. Experimental results will verify the feasibility of the method.

## Introduction

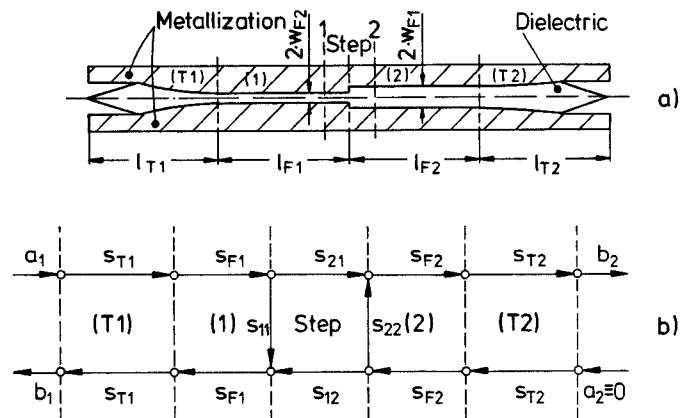
Many techniques are available to calculate the effects of a discontinuity in an unilateral finline [3,4,5,11]. Among these, the scattering matrix solution is perhaps the most commonly used. One of the scattering matrix methods, for analysing discontinuities, involves the determination of equivalent circuits of the discontinuities using the transmission properties of the considered finlines.

Up to now some authors have performed calculations on equivalent circuits of discontinuities in finlines such as: steps, small capacitive strips and inductive notches [3,6,7], but their theoretical results have been derived for an idealized cross sectional model of the finlines [8], i.e. the second order effects such as e.g. the effects of the finite metallization thickness of the fins and the effects of the slits in the finline mounts have been neglected; also the losses caused by the non-ideal dielectric substrate and the finite conductivity of the metallization have not been taken into account.

## Theoretical Background

In this paper, a concept for an efficient calculation method of the scattering matrix of finline discontinuities will be presented, taking into account the above-mentioned second order effects.

A simple step between two finitely long, uniform finlines (1) and (2) which are terminated by smooth tapers (T1) and (T2) on the left- and on the right-hand side is considered (Fig. 1).



**Fig. 1:** Longitudinal section of a finline structure with a step.  
a) The considered finline structure.  
b) The appertaining signal flow diagram.

For the step shown in Fig. 1 the reciprocity theorem is valid:

$$|S_{12}| = |S_{21}| \quad (1)$$

$$\varphi_{12} = \varphi_{21} \quad (2)$$

From the symmetry it follows that:

$$|S_{11}| = |S_{22}| \quad (3)$$

For the finlines yield:

$$S_{F1} = \exp(-a_{F1}l_{F1})\exp(-j\beta_{F1}l_{F1}) \quad (4)$$

$$S_{F2} = \exp(-a_{F2}l_{F2})\exp(-j\beta_{F2}l_{F2}) \quad (5)$$

From the signal flow diagram shown in Fig. 1b) the transmission loss of the complete finline structure shown in Fig. 1a) follows as:

$$a_1 = S_{T1}S_{F1}S_{12}S_{F2}S_{T2} \quad (6)$$

and for the reflection loss:

$$r_1 = S_{T1}^2 S_{F1}^2 S_{11} \quad (7)$$

with the transmission losses  $S_{T1}$  and  $S_{T2}$  of the two tapers (T1) and (T2).

Further, let measurements of the reflection- as well as of the transmission-coefficients have been made for the step feeded at port (1) and port (2) /1/. Then the customary definition of the scattering parameters which describe the step, leads to the equation for the absolute magnitudes of these quantities; e.g. for  $S_{11}$  yields:

$$|S_{11}| = \frac{|r_1|_M}{|S_{T1}|^2 |S_{F1}|^2} \quad (8)$$

with  $r_1|_M$  the measured value of the magnitude of the reflection loss  $r_1$  from (7). Provided that the transmission properties of the applied impedance transformers  $S_{T1}$ ,  $S_{T2}$  between the rectangular waveguide and the homogeneous finline sections and the transmission properties  $S_{F1}$ ,  $S_{F2}$  of the homogeneous finline sections are known, the magnitudes of the other elements of the scattering matrix of the step can similarly be calculated from the measurements.

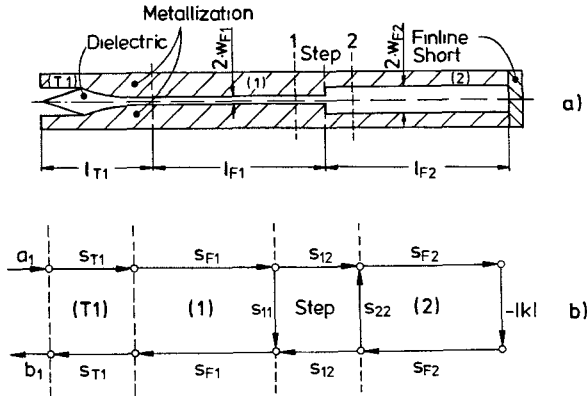


Fig. 2: Longitudinal section of a finline structure with a step and a short circuit.  
a) The considered finline structure.  
b) The appertaining signal flow diagram.

Now, the finline structure shown in Fig. 2a) will be inspected. The reflection loss of the arrangement follows from the appertaining signal flow diagram (Fig. 2b)):

$$r_2' = S_{T1}^2 S_{F1}^2 \left( S_{11} - \frac{|k_2| S_{12}^2 S_{F2}^2}{1 + |k_2| S_{22}^2 S_{F2}^2} \right) \quad (9)$$

whereby  $|k_2| \leq 1$  describes the properties of the finline short.

The phase angles  $\varphi_{11}$ ,  $\varphi_{12}$  and  $\varphi_{22}$  of the considered step scattering parameters will be calculated from the measurements of  $|r_2|$  by the aid of an optimization criterion. Hereby the following equations are valid:

$$E_1 = |r_2'|_C^2 - |r_2'|_M^2 \quad (10)$$

$$E_2 = |r_2''|_C^2 - |r_2''|_M^2 \quad (11)$$

with  $E_1$  and  $E_2$  two error functions which must fulfill the condition:

$$E = E_1^2 + E_2^2 = \text{min. value} \quad (12)$$

whereby  $|r_2'|$  is defined by eq. (9) and  $|r_2''|$  is the reflection loss of the structure shown in Fig. 2 inspected by the right-hand side. The indices C and M stand for the calculated and the measured values of  $|r_2|$ , respectively.

### Numerical and Experimental Results

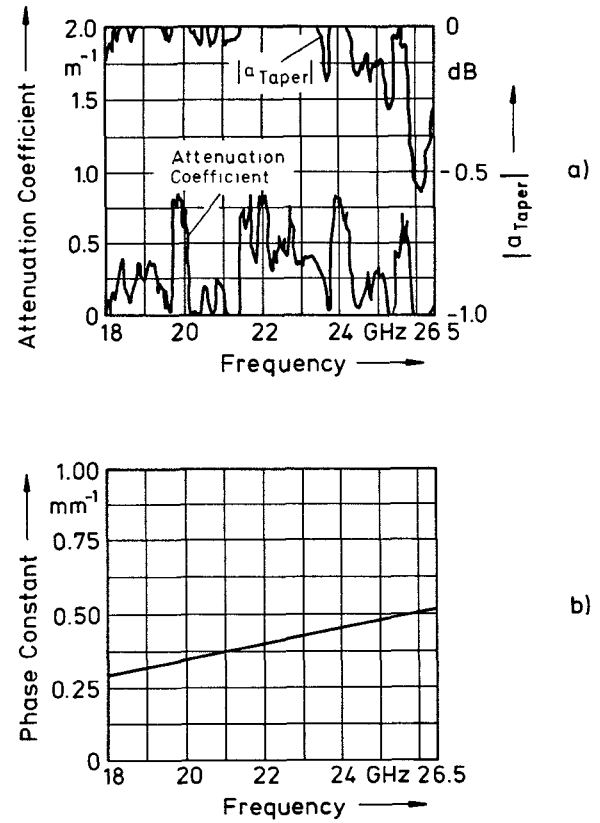


Fig. 3: Transmission properties of a homogeneous finline section with the length  $l_{F1}=240\text{mm}$  and the slotwidth  $2W_F=100\mu\text{m}$  and a single taper section.

- a) The attenuation coefficient of the homogeneous finline section and the damping of a single taper.
- b) The phase constant of the homogeneous finline section.

To calculate the elements of the scattering matrix the properties of the homogeneous finline and of the tapers are needed. Fig. 3a) shows the measured attenuation coefficient for a homogeneous finline with the length  $l_{F1}=240\text{mm}$  and a slot width of  $2W_F=100\mu\text{m}$  which is determined in dependence on the frequency. In Fig. 3b) the calculated values of the phase constant are shown for the same finline. The calculations took into account the finite metallization thickness and the influence of the slits in the finline mounts [2]. Fig. 3a) shows the calculated attenuation for a taper with a length of  $l_T=30\text{mm}$  which is used between the rectangular waveguide and the above described finline structure. Using the results in Fig. 3 and the corresponding results of another finline slot width of  $2W_F=200\mu\text{m}$  and the parameters of the used tapers the magnitudes of the scattering parameters of the finline step can be calculated as a function of the frequency. In Fig. 4 these parameters are shown in dependence on the frequency.

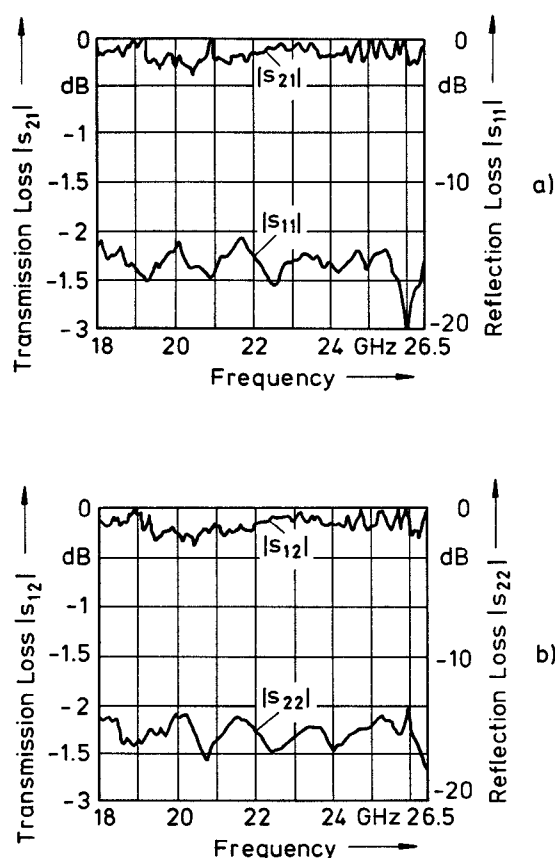


Fig. 4a)-b): The magnitudes of the scattering parameters of a finline step with the slot widths  $2W_{F1}=100\mu\text{m}$  and  $2W_{F2}=200\mu\text{m}$ .

Fig. 5 shows the measured properties of the used finline short, which are used for the optimization process to determine the phase angles. It can be realized that the finline short has a strong frequency dependence.

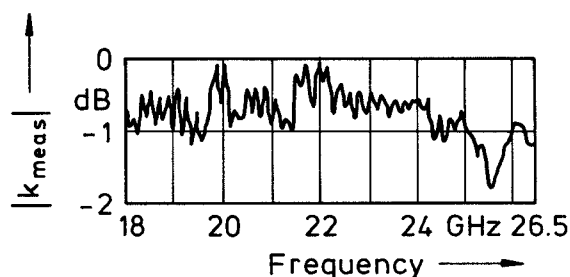


Fig. 5: The reflection loss of the used finline short (see Fig. 2).

The optimized values of the phase angles of the finline step due to the quantities in Fig. 4 are shown in Fig. 6.

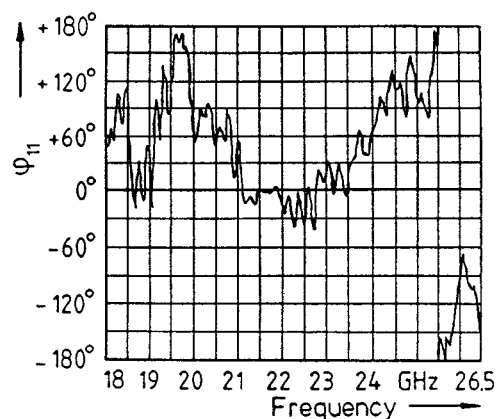
In a similar way discontinuities such as capacitive strips or inductive notches can be investigated and filter structures can be developed. In the continuation of these activities it is scheduled to present and discuss some discontinuities and filter structures.

#### The Measurement Set-Up

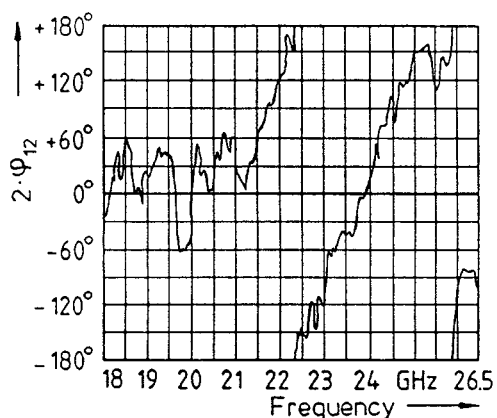
For the design of high-quality millimetre-wave filters in finline technique the exact knowledge of the equivalent circuit elements at the operating frequency is needed [9,10]. Therefore, a measurement technique was developed for determining the transmission properties of the considered discontinuities. The measurement set-up is an automatic system which is steered by a small desk-top computer. The computer controls the measuring frequency, the input power and it stores the measured values. Additionally, the complete optimizing procedure for the evaluation of the measuring results is programmed on the same computer. It should be mentioned that the considered finline discontinuities are lossy two ports. Consequently, all the phase angles of the scattering parameters of the investigated discontinuity must be optimized separately.

#### Conclusions

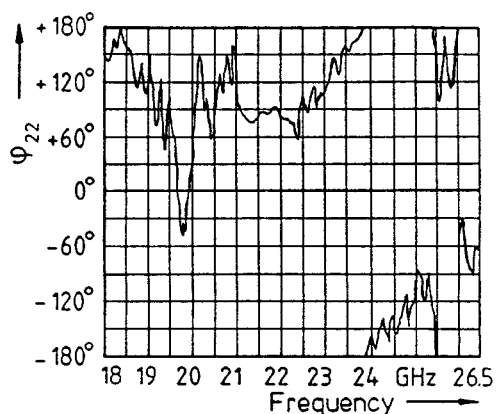
A design method is described which allows a more realistic description of finline discontinuities. In contrast to other methods for equivalent circuits of the finline discontinuities, the present technique takes into account the influence on the transmission properties of both the finite thickness of the fins and the finite longitudinal slit in the waveguide mount as well as the losses of the finline discontinuities.



a)



b)



c)

Fig. 6: The phase angles of a finline step with the slot widths of  $2W_{F1}=100\mu\text{m}$  and  $2W_{F2}=200\mu\text{m}$ .

- a) The phase angle  $\varphi_{11}$ .
- b) The phase angle  $2\varphi_{12}$ .
- c) The phase angle  $\varphi_{22}$ .

## References

- 1) Auda, H. and Harrington, R.: A moment solution for wave guide junctions. IEEE Transactions on Microwave Theory and Techniques, Vol. MTT-31, No. 7, July 1983, pp. 515-519.
- 2) Beyer, A. and Wolff, I.: A solution of the earthed fin line with finite metallization thickness. 1980 IEEE MTT-S International Symposium Digest, Washington, D.C., pp. 258-260.
- 3) El Hennawy, H. and Schünemann, K.: Hybrid fin-line matching structures. IEEE Transactions on Microwave Theory and Techniques, Vol. MTT-30, December 1982, pp. 2132-2138.
- 4) El Hennawy, H. and Schünemann, K.: Impedance transformation in fin-lines. IEE Proc. Part H, No. 6, Microwaves, Optics and Antennas, Vol.129, December 1982, pp. 342-350.
- 5) Helard, M., Citerne, J., Picon, O. and Fouad Hanna, V.: Exact calculations of scattering parameters of a step slot width discontinuity in an unilateral fin-line. Electronics Letters, 7th July 1983, Vol. 19, No. 14, pp. 537-539.
- 6) Konishi, Y. and Uenakada, K.: The design of a bandpass filter with inductive strip-planar circuits mounted in waveguide. IEEE Transactions on Microwave Theory and Techniques, Vol. MTT-22, October 1974, pp. 869-873.
- 7) Meier, P.J.: Integrated fin-line millimeter components. IEEE Transaction on Microwave Theory and Techniques, Vol. MTT-22, December 1974, pp. 1209-1216.
- 8) Schmidt, L.-P.: A comprehensive analysis of quasiplanar waveguides for millimeter-wave applications. Proc. of the 11th European Microwave Conference, Amsterdam (NL), 1981, pp. 315-320.
- 9) Tajima, Y. and Sawayama, Y.: Design and analysis of a waveguide-sandwich microwave filter. IEEE Transaction on Microwave Theory and Techniques, Vol. MTT-22, September 1974, pp. 839-841.
- 10) Taub, J.J.: Design of minimum loss band-pass filters. Microwave Journal, Vol. 6, 1963, pp. 67-76.
- 11) Webb, K. J.: Mittra, R.: A variational solution of the fin-line discontinuity problem. Proc. of the 15th European Microwave Conference, Paris (F), 1985, pp. 311-316.